



# Quantum matter out of equilibrium - pathway to technological breakthrough?

**Patryk Kubiczek**

PhD student / research assistant

University of Hamburg

# Achievements of quantum physics: highlights

- **Transistor**  
(1947, Bardeen, Brattain, and Shockley, 1956 Nobel Prize in Physics)
- **Superconductivity**  
(1911, Kammerlingh-Onnes, 1913 Nobel Prize in Physics;  
theory: 1957, Bardeen, Cooper, and Schrieffer, 1972 Nobel Prize in Physics)
- **High-temperature superconductivity**  
(1986, Bednorz and Müller, 1987 Nobel Prize in Physics)
- **Nuclear magnetic resonance**  
(molecules: 1938, Rabi, 1944 Nobel Prize in Physics;  
solids: 1946, Bloch and Purcell, 1952 Nobel Prize in Physics)
- **Magnetic resonance imaging (MRI)**  
(1973, Lauterbur and Mansfield,  
2003 Nobel Prize in Physiology or Medicine)



modern MRI scanner

# Challenges

- Next-generation electronics
  - ultrafast control
  - miniaturization
- Transformation of energy system
  - new sources of clean energy
  - efficient photovoltaic solar cells
  - improved energy storage and transmission
  - smart technologies for energy savings



silicon solar cell

# Strongly correlated electronic systems: *Quantum Matter*

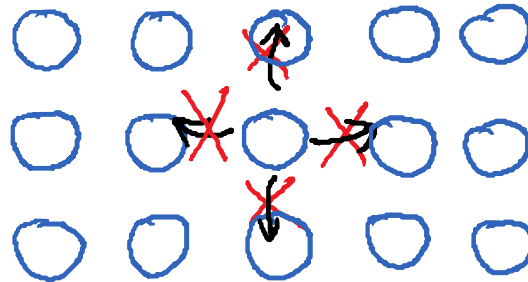
Group →	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	
Period ↓																			
1	1 H																		2 He
2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne	
3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar	
4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr	
5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe	
6	55 Cs	56 Ba	57 La *	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn	
7	87 Fr	88 Ra	89 Ac *	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og	
				* 58 Ce	* 59 Pr	* 60 Nd	* 61 Pm	* 62 Sm	* 63 Eu	* 64 Gd	* 65 Tb	* 66 Dy	* 67 Ho	* 68 Er	* 69 Tm	* 70 Yb	* 71 Lu		
				* 90 Th	* 91 Pa	* 92 U	* 93 Np	* 94 Pu	* 95 Am	* 96 Cm	* 97 Bk	* 98 Cf	* 99 Es	* 100 Fm	* 101 Md	* 102 No	* 103 Lr		

## ■ Examples:

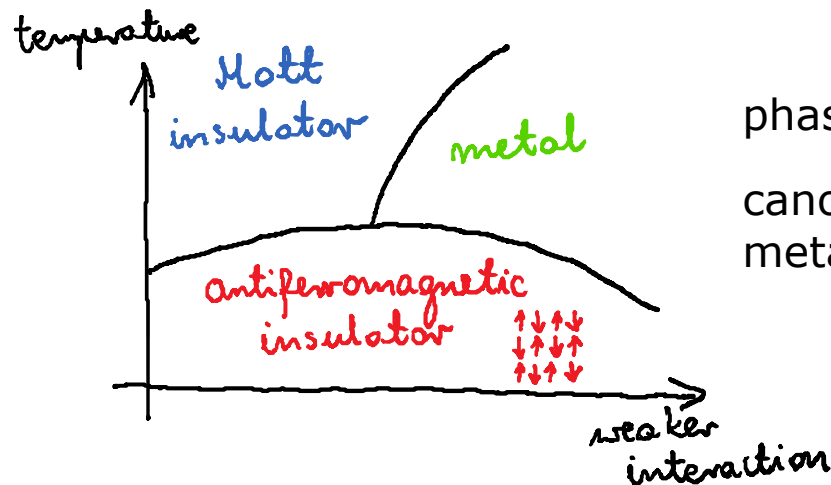
- Mott insulators (transition metal oxides,  $V_2O_3$ )
- high-temperature superconductors (cuprates,  $YBa_2Cu_3O_{7-x}$ )
- heavy-fermion materials (rare-earth and actinide compounds,  $UGe_2$ )

# Mott insulator

- Theoretical concept: 1937, Nevill F. Mott, 1977 Nobel Prize in Physics (1/3)
- Electrons frozen in their equilibrium positions due to Coulombic repulsion



- No transfer of charge possible
- Transition to metallic state when interaction strength decreased



phase diagram of  $V_2O_3$

canonical example of Mott metal-insulator transition

## Mott insulator *out of equilibrium*

- Control of metal-insulator transitions by electric pulses: possibility to build resistive random-access memory (ReRAM)

[L. Cario , C. Vaju , B. Corraze , V. Guiot , E. Janod , Adv. Mater., 225193 (2010)]



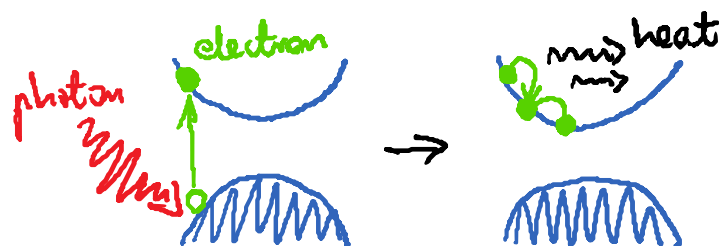
- Metastable hidden quantum states induced by laser pulses: another possibility for ReRAM

[L. Stojchevska et al., *Science* 344, 177 (2014)]

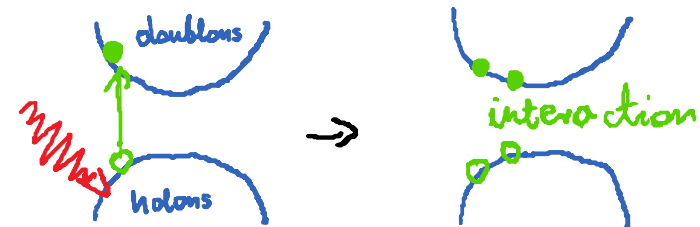
 long lived nonequilibrium state ( $\sim 10^{-2}$  s)  
35 fs ( $10^{-15}$  s)

- Solar-light driven Mott insulator: efficient photovoltaic device

[E. Manousakis, Phys. Rev. B 82, 125109 (2010)]



silicon solar cell



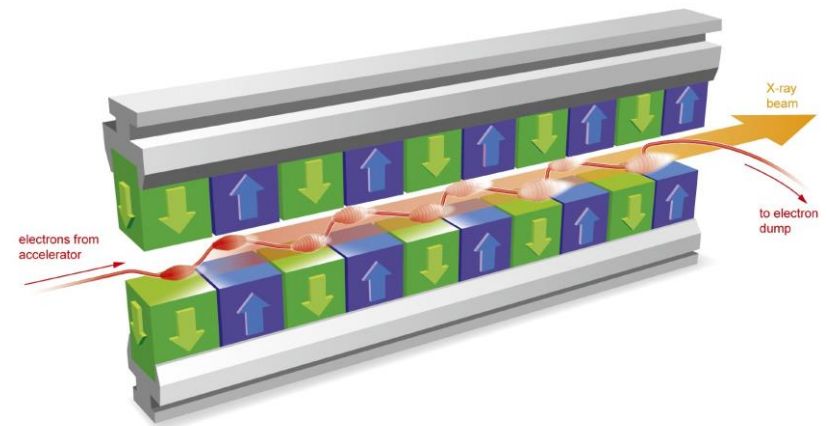
Mott insulator solar cell

# Europen X-Ray Free Electron Laser (XFEL)

- Source of ultrashort and ultra intense X-ray laser pulses
- Enables the study of real-time atomic-scale ultrafast dynamics of complex materials and biomolecules
- Official inauguration: 1 September 2017



total length = 3,4 km  
electron accelerator: 2,1 km  
undulators: 125 m, 212 m



# Theoretical description: Solving many-body quantum problem

- Classical systems can be only in one state at a time
- Quantum systems can be in a superposition of many different states





$$\psi(t) = \sum_i^M c_i(t) \phi_i$$

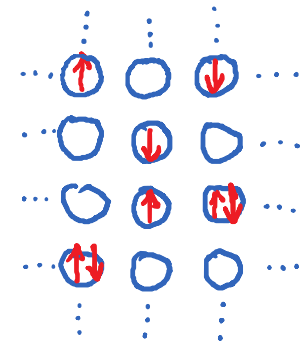
- Goal: find probability amplitudes  $c_i(t)$  by solving Schrödinger equation

$$i \frac{\partial}{\partial t} \psi(t) = H(t) \psi(t)$$

- In practice infeasible: example – Hubbard model

– each site can be in one of 4 states:

- empty 
- occupied by spin-up electron 
- occupied by spin-down electron 
- doubly occupied 



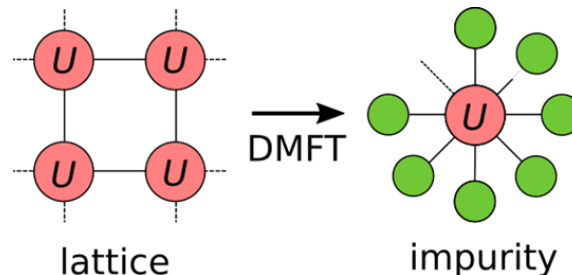
– whole system of  $N$  sites can be in  $M = 4^N$  states

–  $N = 10^{23}$ , then  $M = 4^{10^{23}} \gg 10^{80}$  – number of atoms in the Universe



## Theoretical description: approximations needed

- By neglecting interactions the electronic wavefunction factorizes: single-electron instead of many-electron problem (-> DFT)
- Not possible for strongly correlated systems: do some kind of mean field theory instead (-> DMFT)



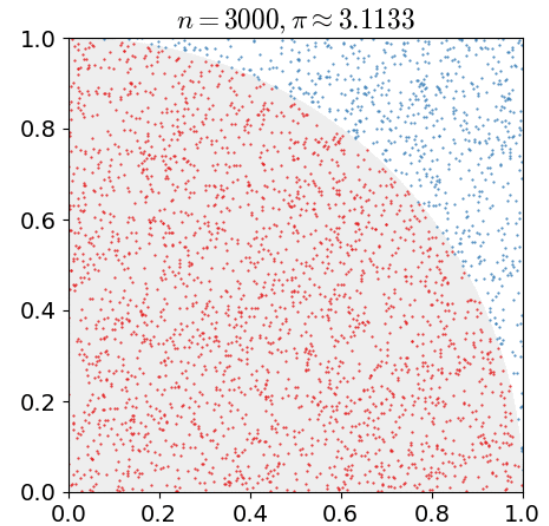
- Now solve the impurity problem: electrons interact only on the central site
- Idea:
  - solve the central site ( $M = 4$ ) and bath (single-particle) separately
  - find the correction to the result for the full system by summing up all Feynman diagrams
  - there are too many Feynman diagrams to do this diagram-by-diagram
  - select diagrams randomly based on their importance: Monte Carlo

# Quantum Monte Carlo

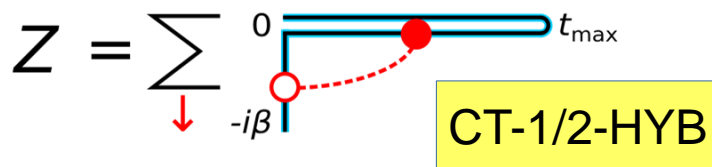
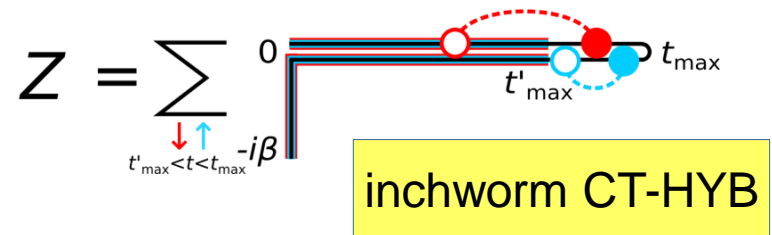
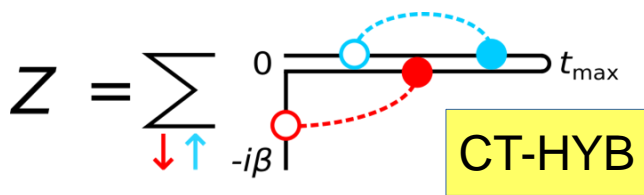
- Monte Carlo: stochastic way to evaluate integrals
- Example: area of a circle

$$f(x, y) = \begin{cases} 1 \\ 0 \end{cases}$$

$$\int_0^1 dx \int_0^1 dy f(x, y) = \frac{\pi}{4}$$



- Quantum Monte Carlo: stochastic way to sum Feynman diagrams



# Summary

---

- Quantum physics underlies many of the modern technologies
  - electronics
  - medical imaging (MRI)
- Strongly correlated electronic systems
  - fascinating macroscopic quantum phenomena (Mott insulators, high-temperature superconductors, ...)
  - theoretical description challenging
  - possibilities for technological applications
- Nonequilibrium physics is an active field of research
  - European XFEL in Hamburg

---

# Thank you for your attention!

## References (for experts):

- H. Aoki et al., Nonequilibrium dynamical mean-field theory and its applications, Rev. Mod. Phys. **86**, 779 (2014)
- E. Gull et al., Continuous-time Monte Carlo methods for quantum impurity models, Rev. Mod. Phys. **83**, 349 (2011)
- E. Janod et al., Resistive Switching in Mott Insulators and Correlated Systems, Adv. Funct. Mater. **25**, 6287 (2015)

Support from SFB925 gratefully acknowledged

