

# Ferromagnetism and spin triplet superconductivity in $UGe_2$

Patryk Kubiczek

Jagiellonian University in Kraków

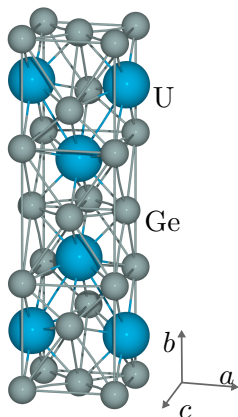


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# Introduction

- ▶ In 2000 Saxena *et al.* reported on a superconductivity inside the ferromagnetic phase of  $\text{UGe}_2$
- ▶ Coexistence with ferromagnetism implies spin-triplet superconductivity, unlike in the BCS theory
- ▶ Until today only three ferromagnetic superconductors have been discovered:  $\text{UGe}_2$ ,  $\text{UCoGe}$ ,  $\text{URhGe}$
- ▶ All of them are so called heavy-fermion compounds
- ▶ The key ingredient in understanding their physics are unfilled  $5f$  levels of the uranium atoms
- ▶ I will discuss a possible effective microscopic model for magnetism and superconductivity in  $\text{UGe}_2$

# Crystal structure



- ▶ primitive cell size  
 $(a, b, c) = (0.40, 1.51, 0.41) \text{ \AA}$
- ▶ orthorhombic centrosymmetric crystal system
- ▶ spontaneous magnetization along  $a$  axis
- ▶  $[U] = [Rn] 5f^3 3d^1 7s^2$
- ▶  $[Ge] = [Ar] 3d^{10} 4s^2 4p^2$

Figure: Primitive cell of  $UGe_2$

# Phase diagram

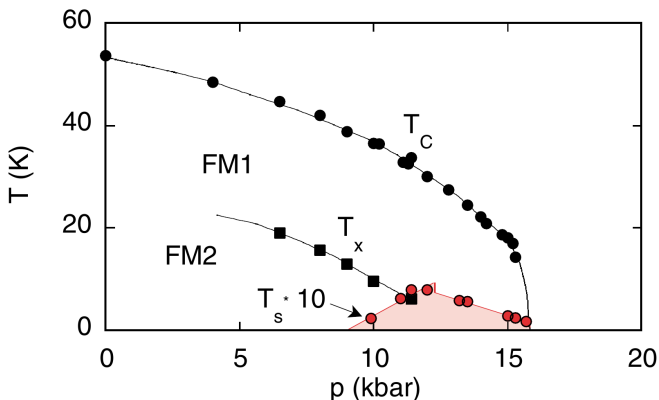


Figure: Pressure-temperature phase diagram (Pfleiderer 2002)

For  $p = 1.2$  GPa:  $T_{sc} = 0.8$  K,  $T_C = 30$  K

# Magnetization

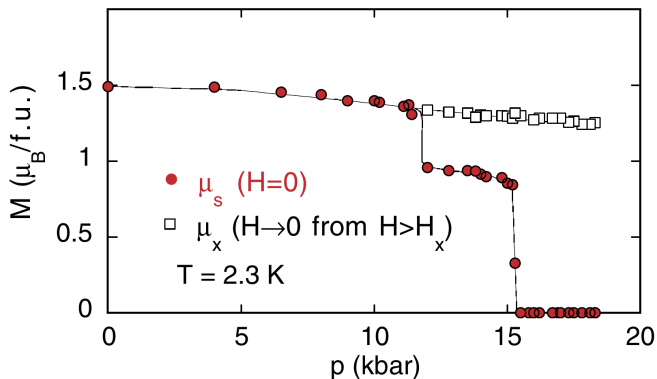


Figure: Magnetization vs. pressure (Pfleiderer 2002)

# Band structure

- ▶ Band structure calculations can explain the ordered moment
- ▶ However they fail to properly describe the Fermi surface

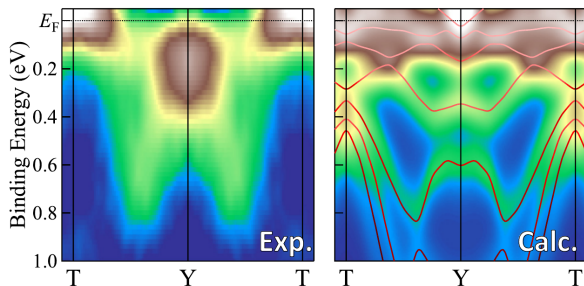


Figure: Angle-resolved photoemission spectroscopy results (Fujimori 2015)

- ▶ De Haas - van Alphen oscillation experiments indicate quasi 2-dimensional character

# Anderson lattice model

$$H = \sum_{ij\sigma} t_{ij} c_{i\sigma}^\dagger c_{j\sigma} + \epsilon_f \sum_{i\sigma} \hat{n}_{i\sigma}^f + U \sum_i \hat{n}_{i\uparrow}^f \hat{n}_{i\downarrow}^f \\ + \sum_{i\sigma} \left( V c_{i\sigma}^\dagger f_{i\sigma} + V^* f_{i\sigma}^\dagger c_{i\sigma} \right)$$

- ▶ Effective model describing hybridization of initially localized  $f$ -electrons with mobile conduction electrons
- ▶ Strong Coulomb interaction between  $f$  electrons "pins" magnetic moments to  $f$ -levels
- ▶ Popular model for heavy-fermion compounds explaining the origin of large effective masses due to peaks in the density of states

# Gutzwiller approximation

- ▶ Ansatz wavefunction

$$|\Psi_G\rangle = \prod_i \hat{P}_i |\Psi_0\rangle$$

$$\hat{P}_i = 1 - (1 - g) \hat{n}_{i\uparrow}^f \hat{n}_{i\downarrow}^f$$

- ▶ Approximate evaluation of observables (exact for  $D = \infty$ )

$$\langle \Psi_G | \mathcal{O}_i | \Psi_G \rangle \approx \langle \Psi_0 | \hat{P}_i \mathcal{O}_i \hat{P}_i | \Psi_0 \rangle$$

- ▶ One can express  $g$  as a function of  $d^2 = \langle \hat{n}_{i\uparrow}^f \hat{n}_{i\downarrow}^f \rangle$



# Statistically-consistent Gutzwiller approximation

- ▶ Assume particular  $n_f = \langle \hat{n}_{i\uparrow}^f + \hat{n}_{i\downarrow}^f \rangle_0$  and  $m_f = \langle \hat{n}_{i\uparrow}^f - \hat{n}_{i\downarrow}^f \rangle_0$  of the Fermi-sea state  $|\Psi_0\rangle$
- ▶ Introduce Lagrange multipliers to assure  $n_f = \langle \hat{n}_f \rangle$  and  $m_f = \langle \hat{m}_f \rangle$
- ▶ Finding the optimal parameters is equivalent to solving the following free Hamiltonian and minimizing ground state energy with respect to set  $\{d, n_f, m_f, \lambda_n^f, \lambda_m^f\}$

$$H_{SGA} = \sum_{\mathbf{k}\sigma} \begin{pmatrix} c_{\mathbf{k}\sigma}^\dagger & f_{\mathbf{k}\sigma}^\dagger \end{pmatrix} \begin{pmatrix} \epsilon_{\mathbf{k}}^c - \mu & \sqrt{q_\sigma} V \\ \sqrt{q_\sigma} V & \epsilon_f - \mu - \lambda_n^f - \sigma \lambda_m^f \end{pmatrix} \begin{pmatrix} c_{\mathbf{k}\sigma} \\ f_{\mathbf{k}\sigma} \end{pmatrix} + N(Ud^2 + \lambda_n^f n^f + \lambda_m^f m^f)$$

# Results

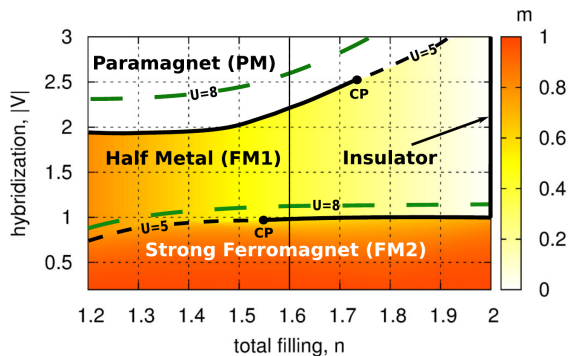
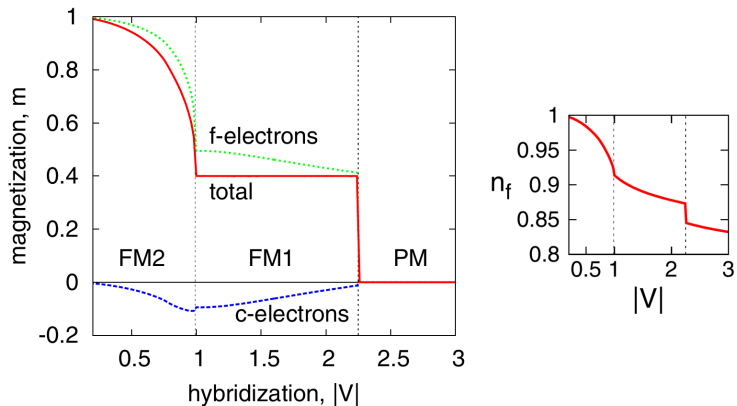


Figure: Magnetization on the filling-hybridization plane (Wysokiński 2014)

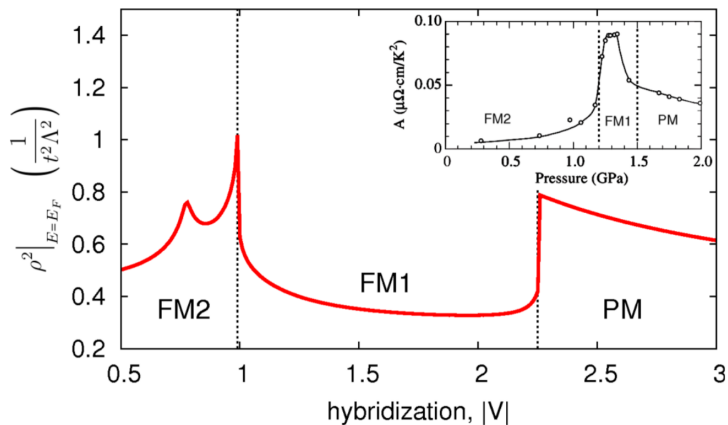
- ▶ Pressure affects parameters of the model in an unknown way
- ▶ It is assumed  $V$  is a monotonically increasing function of  $p$

# Magnetization and $f$ -filling



**Figure:** Magnetization and  $n_f$  as a function of hybridization (Wysockiński 2014)

# Density of states at Fermi energy



**Figure:** Square of DOS at  $E_F$  vs.  $V$ , inset: coefficient  $A$  of  $T^2$  term of resistivity vs. pressure (Wysokiński 2014)

# Gap function symmetry - general properties

- ▶ The gap function must be antisymmetric under the exchange of fermionic indices

$$\langle f_{\mathbf{k}\sigma} f_{-\mathbf{k}\sigma} \rangle \sim \Delta_{\sigma\sigma'}(\mathbf{k}) = -\Delta_{\sigma'\sigma}(-\mathbf{k})$$

- ▶ Spin-triplet state is symmetric in spin space so the spatial part needs to be antisymmetric
- ▶ However we introduce additional degenerate  $f$ -level so the gap function is parametrized by more indices,  $l, l' \in \{1, 2\}$

$$\langle f_{\mathbf{k}l\sigma} f_{-\mathbf{k}l'\sigma} \rangle \sim \Delta_{\sigma\sigma'}^{ll'}(\mathbf{k}) = -\Delta_{\sigma'\sigma}^{l'l}(-\mathbf{k})$$

# Gap function symmetry assumed in the model

- ▶ We consider spin-triplet, orbital-singlet *s*-wave pairing in the equal-spin channel:

$$\Delta^{ll'}(\mathbf{k}) = \begin{pmatrix} \Delta_{\uparrow\uparrow}^{ll'} & 0 \\ 0 & \Delta_{\downarrow\downarrow}^{ll'} \end{pmatrix}$$

$$\Delta^{ll'}(\mathbf{k}) = -\Delta^{l'l}(\mathbf{k})$$

- ▶ This type of spin-triplet pairing is favoured by Hund's rule coupling between the two *f*-levels (Spaček 2001)

# Degenerate Anderson lattice model

- ▶ When additional  $c$  and  $f$ -levels are introduced the inter-orbital Coulomb interactions are included in the Hamiltonian

$$\begin{aligned}
 H = & \sum_{ijl\sigma} t_{ij} c_{il\sigma}^\dagger c_{jl\sigma} + \epsilon_f \sum_{il\sigma} \hat{n}_{il\sigma}^f + U \sum_{il} \hat{n}_{il\uparrow}^f \hat{n}_{il\downarrow}^f \\
 & + \sum_{il\sigma} \left( V c_{il\sigma}^\dagger f_{il\sigma} + V^* f_{il\sigma}^\dagger c_{il\sigma} \right) \\
 & + \frac{1}{2} U' \sum_{ill'} \hat{n}_{il}^f \hat{n}_{il'}^f - J \sum_{ill'} \left( \mathbf{s}_{il}^f \mathbf{s}_{il'}^f + \frac{1}{4} \hat{n}_{il}^f \hat{n}_{il'}^f \right)
 \end{aligned}$$

# Pairing operators

- ▶ The inter-orbital part of the Hamiltonian equals

$$\frac{1}{2}(U' + J) \sum'_{ill'} B_{ill'}^\dagger B_{ill'} + \frac{1}{2}(U' - J) \sum'_{ill'} \mathbf{A}_{ill'}^\dagger \mathbf{A}_{ill'}$$

$$B_{ill'} \equiv \frac{1}{\sqrt{2}} (f_{il\uparrow} f_{il'\downarrow} - f_{il\downarrow} f_{il'\uparrow})$$

$$\mathbf{A}_{ill'} \equiv \left( f_{il\uparrow} f_{il'\uparrow}, \frac{1}{\sqrt{2}} (f_{il\uparrow} f_{il'\downarrow} + f_{il\downarrow} f_{il'\uparrow}), f_{il\downarrow} f_{il'\downarrow} \right)$$

- ▶ Thus if  $U' < J$  spin-triplet condensation will lower the energy
- ▶ We assume  $U' = U - 2J$



# Mean-field approximation

- ▶ We analyze the coexisting ferromagnetism and superconductivity by mean-field decoupling

$$\mathcal{O}_\alpha \mathcal{O}_\beta \rightarrow \langle \mathcal{O}_\alpha \rangle \mathcal{O}_\beta + \mathcal{O}_\alpha \langle \mathcal{O}_\beta \rangle - \langle \mathcal{O}_\alpha \rangle \langle \mathcal{O}_\beta \rangle$$

- ▶ We look for self-consistent solutions for the following parameters

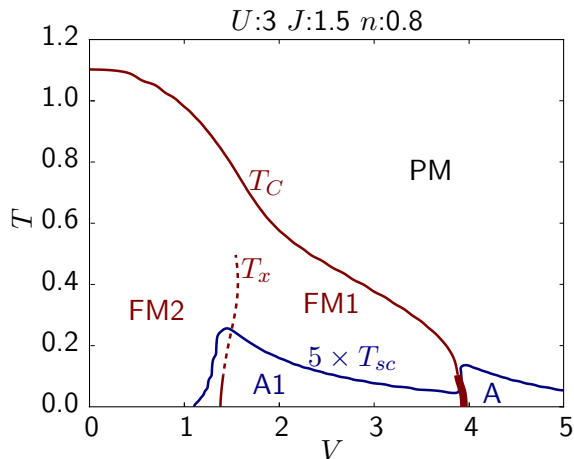
$$n_f = \langle \hat{n}_1^f \rangle = \langle \hat{n}_2^f \rangle$$

$$m_f = \langle \hat{m}_1^f \rangle = \langle \hat{m}_2^f \rangle$$

$$\Delta_\uparrow = (U' - J) \langle f_{\mathbf{k}1\uparrow} f_{-\mathbf{k}2\uparrow} \rangle$$

$$\Delta_\downarrow = (U' - J) \langle f_{\mathbf{k}1\downarrow} f_{-\mathbf{k}2\downarrow} \rangle$$

# Phase diagram



A1:

$$\Delta_{\uparrow} = 0, \Delta_{\downarrow} \neq 0$$

A:

$$\Delta_{\uparrow} = \Delta_{\downarrow} \neq 0$$

Figure: Phase diagram in MF approximation

# Magnetization and superconducting gap

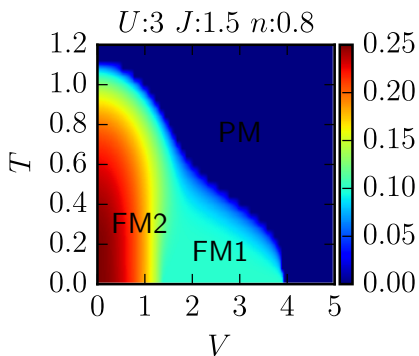


Figure: Magnetization  $m$

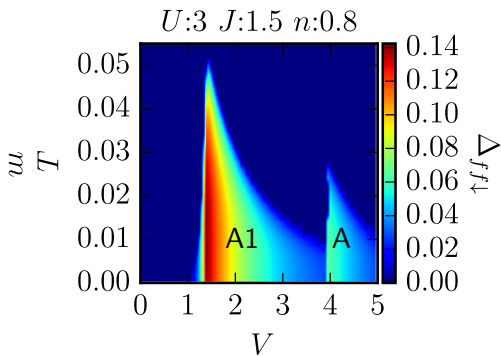


Figure: Superconducting gap  $\Delta_{\downarrow}$

$$m = \frac{1}{2}(m_f + m_c)$$

# Magnetization, filling

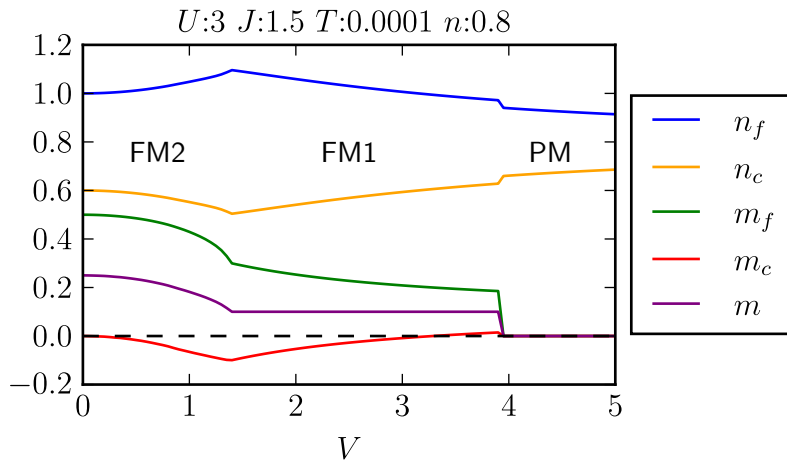


Figure: Magnetization and filling of  $c$  and  $f$ -levels

# Superconductivity

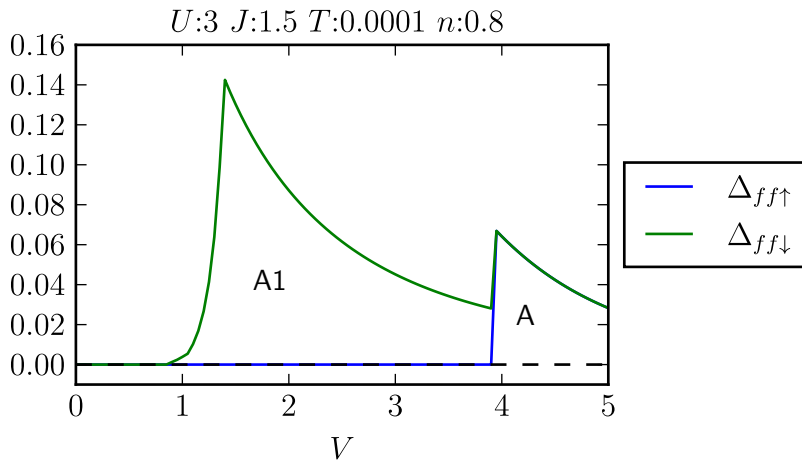


Figure: Superconducting gaps

# DOS evolution at the FM2-FM1 transition

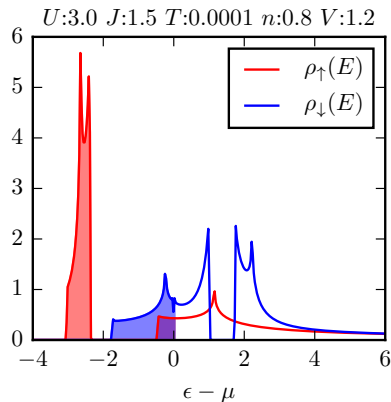


Figure: DOS in FM2 phase

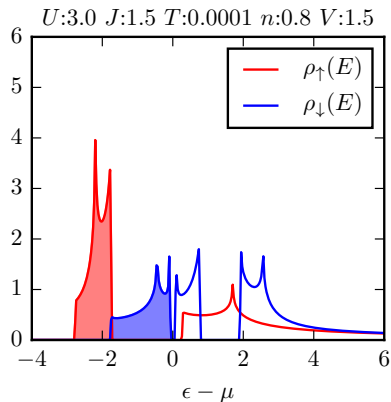


Figure: DOS in FM1 phase

# DOS evolution at the FM1-PM transition

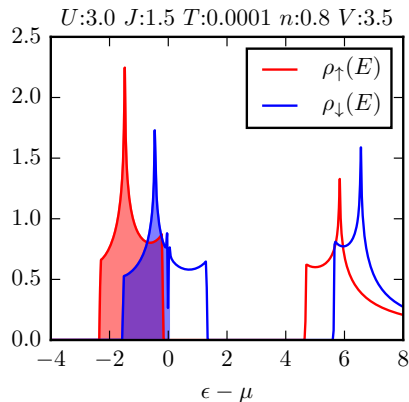


Figure: DOS in FM1 phase

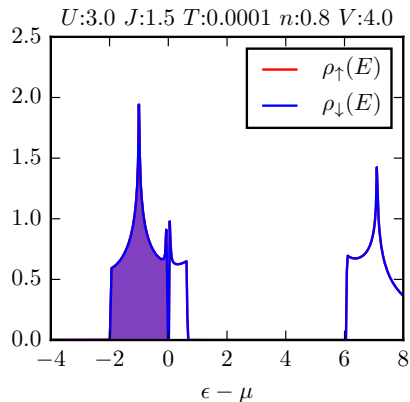


Figure: DOS in PM phase

# Summary







- ▶ Anderson lattice model away from half-filling can account for the qualitative description of the phases of  $UGe_2$
- ▶ The degenerate version of the model predicts interorbital spin-triplet pairing due to Hund's rule at the mean-field level
- ▶ Whether such a simplified model is a good microscopic description of  $UGe_2$  remains an open question



Thank you for your attention!



# References

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